- 1. **Spatial Velocity:** A cylinder rolls without slipping in the  $\hat{x}_0$  direction on the  $\hat{x}_0 \hat{y}_0$  plane. The cylinder has a radius of r and a constant forward speed of v. Let  ${}^{0}C = [C_x(t), 0, 0]^T$  be the position of the contact point at time t. Let  ${}^{0}A = [A_x(t), 0, 0]^T$  be the position of the instantaneous top of the cylinder at time t.
  - (a) What is the linear velocity of the point C? (hint: just need to compute  $\frac{d}{dt}C_x(t)$ )?
  - (b) What is the linear velocity of the point A?
  - (c) What is velocity of the body-fixed point currently coincides with C?
  - (d) What is velocity of the body-fixed point currently coincides with A?
  - (e) What is the spatial velocity of the cylinder in  $\{0\}$ -frame?
  - (f) What is the spatial velocity of the cylinder in frame  $\{C\}$ ? ( $\{C\}$  has the same orientation as  $\{0\}$ , while its origin is at the contact point C)

Note: The first 4 questions are all referring to the inertia frame  $\{0\}$ 



- 2. Modern Robotics: Exercise 3.21
- 3. Modern Robotics: Exercise 3.28
- 4. Modern Robotics: Exercise 5.5
- 5. Modern Robotics: Exercise 5.6